

A New Initialization Scheme of the ZUC-256 Stream Cipher

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Abstract. ZUC-256 stream cipher, together with AES-256 and SNOW 5G, are specified as the future 3GPP confidentiality and integrity algorithms for the air interface by SAGE recently. In this short paper, we describe a new initialization scheme of ZUC-256 with 48 rounds that supports an IV of the exact 128 bits as a positive response to SAGE's recommendation. Compared to the original initialization scheme, this new key/IV setup algorithm avoids the division of the whole key/IV byte and provides a simple and natural-looking initialization scheme for ZUC-256 with a large expected security margin.

Keywords: 5G, Stream ciphers, ZUC, 256-bit security.

1 Introduction

The core of the 3GPP confidentiality and integrity algorithms 128-EEA3 and 128-EIA3 is the ZUC-128 stream cipher [1]. ZUC-256 is a new member in the ZUC family of stream ciphers, formally proposed in 2018 for the intended usage in the upcoming 5G applications for 3GPP. ZUC-256 stream cipher is industrial-friendly, differing from ZUC-128 only in the initialization phase and in the message authentication codes (MAC) generation phase. The first publicized version of ZUC-256 works with a 256-bit key and a 184-bit initialization vector (IV) and generates a keystream frame of length from 20000 to 2^{32} bits after each mixture of the (key, IV) pair.

After the publication of ZUC-256, there is an increasing interest of evaluating its security against various cryptanalytic approaches. At the ZUC-256 international conference in 2018 [7], there are several talks that analyzed different aspects of its security, all of which imply that ZUC-256 is secure against the corresponding cryptanalysis method. Then, a linear distinguishing attack is presented in [5] at FSE 2020, requiring an exceptionally-long keystream frame, which is out of the security claim in [8], as analyzed in [6]. For the analysis of the initialization phase, there is a differential analysis published in [4] and a new cryptanalysis result using modular differences in [3]. In November 2022, SAGE has released a new liaison [2] which specifies AES-256, SNOW 5G and ZUC-256 as the 3GPP 256-bit Confidentiality and Integrity Algorithms for the Air interface and gives the recommendation on ZUC-256 to work with a 48-round

of initialization scheme for a large expected security margin, compared to the scheme presented in [9].

As a positive response to SAGE's recommendation, we propose a new initialization scheme of ZUC-256 that works with a 256-bit key and a 128-bit IV which goes through a 48-round initialization scheme in this paper. This new key/IV setup scheme avoids the division of the whole key/IV byte, is simple and natural-looking, and also provides the 256-bit security in 5G applications with a large expected security margin. A brief cryptanalysis of the new initialization scheme is also yielded.

This paper is structured as follows. In Section 2, we give the detailed description of ZUC-256 with the new initialization scheme. The cryptanalysis related to the new introduced change will be discussed in Section 3. Finally, some conclusions are drawn in Section 4.

2 The Description of the New Initialization Scheme for ZUC-256

In this section, we will present the detailed description of the new initialization scheme of ZUC-256 stream cipher. The following notations will be used hereafter.

- Denote the integer modular addition by \oplus , i.e., for $0 \leq x < 2^{32}$ and $0 \leq y < 2^{32}$, $x \oplus y$ is the integer addition mod 2^{32} .
- Denote the integer addition modulo $2^{31} - 1$ by $x + y \bmod (2^{31} - 1)$ for $1 \leq x \leq 2^{31} - 1$ and $1 \leq y \leq 2^{31} - 1$.
- Denote the bitwise exclusive OR by \oplus .
- Denote the bit string concatenation by \parallel .
- $K = (K_{31}, K_{30}, \dots, K_2, K_1, K_0)$, the 256-bit secret key used in the ZUC-256 where K_i for $0 \leq i \leq 31$ are 8-bit bytes.
- $IV = (IV_{15}, \dots, IV_1, IV_0)$, the 128-bit initialization vector used in the ZUC-256 where IV_i for $0 \leq i \leq 15$ are 8-bit bytes.
- d_i for $0 \leq i \leq 15$ are the 7-bit constants used in the ZUC-256 stream cipher.
- $\ll n$, the left rotation of a 64-bit operand, $x \ll n$ means $((x \ll n) \oplus (x \ll (64 - n)))$.

As depicted in Fig.1, there are 3 parts involved in ZUC-256: a 496-bit linear feedback shift register (LFSR) defined over the field $GF(2^{31} - 1)$, consisting of 16 31-bit cells $(s_{15}, s_{14}, \dots, s_2, s_1, s_0)$ defined over the set $\{1, 2, \dots, 2^{31} - 1, g\}$; a bit reorganization layer (BR), which extracts the content of the LFSR to form 4 32-bit words, (X_0, X_1, X_2, X_3) , used in the following finite state machine (FSM);

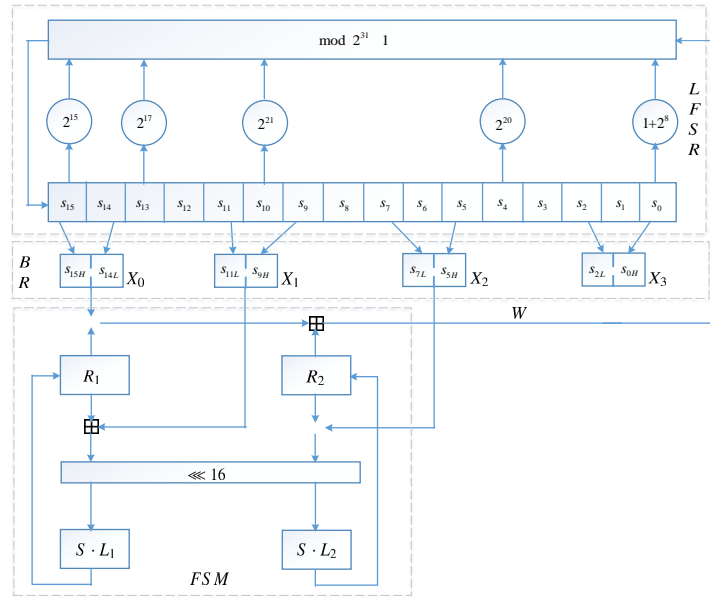


Fig. 1. The initialization phase of the ZUC-256 stream cipher

The Key/IV loading scheme is as follows.

$$\begin{aligned}
 s_0 &= K_0 \ k \ d_0 \ k \ K_{16} \ k \ K_{24} \\
 s_1 &= K_1 \ k \ d_1 \ k \ K_{17} \ k \ K_{25} \\
 s_2 &= K_2 \ k \ d_2 \ k \ K_{18} \ k \ K_{26} \\
 s_3 &= K_3 \ k \ d_3 \ k \ K_{19} \ k \ K_{27} \\
 s_4 &= K_4 \ k \ d_4 \ k \ K_{20} \ k \ K_{28} \\
 s_5 &= K_5 \ k \ d_5 \ k \ K_{21} \ k \ K_{29} \\
 s_6 &= K_6 \ k \ d_6 \ k \ K_{22} \ k \ K_{30} \\
 s_7 &= K_7 \ k \ d_7 \ k \ IV_0 \ k \ IV_8 \\
 s_8 &= K_8 \ k \ d_8 \ k \ IV_1 \ k \ IV_9 \\
 s_9 &= K_9 \ k \ d_9 \ k \ IV_2 \ k \ IV_{10} \\
 s_{10} &= K_{10} \ k \ d_{10} \ k \ IV_3 \ k \ IV_{11} \\
 s_{11} &= K_{11} \ k \ d_{11} \ k \ IV_4 \ k \ IV_{12} \\
 s_{12} &= K_{12} \ k \ d_{12} \ k \ IV_5 \ k \ IV_{13} \\
 s_{13} &= K_{13} \ k \ d_{13} \ k \ IV_6 \ k \ IV_{14} \\
 s_{14} &= K_{14} \ k \ d_{14} \ k \ IV_7 \ k \ IV_{15} \\
 s_{15} &= K_{15} \ k \ d_{15} \ k \ K_{23} \ k \ K_{31},
 \end{aligned}$$

where the constants d_i for $0 \leq i \leq 15$ are defined as follows, which are based on the binary expansion of π including the integer part.

$$\begin{aligned} d_0 &= 1100100 \\ d_1 &= 1000011 \\ d_2 &= 1111011 \\ d_3 &= 0101010 \\ d_4 &= 0010001 \\ d_5 &= 0000101 \\ d_6 &= 1010001 \\ d_7 &= 1000010 \\ d_8 &= 0011010 \\ d_9 &= 0110001 \\ d_{10} &= 0011000 \\ d_{11} &= 1100110 \\ d_{12} &= 0010100 \\ d_{13} &= 0101110 \\ d_{14} &= 0000001 \\ d_{15} &= 1011100. \end{aligned}$$

Note that there is no hidden weakness introduced in the above constants. There are $48 + 1 = 49$ rounds of initialization in this new key/IV setup scheme of ZUC-256, which is depicted as follows.

1. Load the key, IV and constants into the LFSR as specified above.
2. Let $R_1 = R_2 = 0$.
3. for $i = 0$ to 47 do
 - { Bitreorganization()
 - { $W = F(X_0, X_1, X_2)$
 - { LFSRWithInitializationMode($W \ll 1$)
4. { Bitreorganization()
 - { $W = F(X_0, X_1, X_2)$ and discard W
 - { LFSRWithworkMode().

Now we specify the relevant subroutines one-by-one.

LFSRWithInitializationMode(u)

1. $v = 2^{15} s_{15} + 2^{17} s_{13} + 2^{21} s_{10} + 2^{20} s_4 + (1 + 2^8) s_0 \bmod(2^{31} - 1)$
2. if $v = 0$ then set $v = 2^{31} - 1$
3. $s_{16} = v + u \bmod(2^{31} - 1)$
4. if $s_{16} = 0$ then set $s_{16} = 2^{31} - 1$
5. $(s_{16}, s_{15}, \dots, s_2, s_1) \leftarrow (s_{15}, s_{14}, \dots, s_1, s_0)$.

LFSRWithworkMode()

1. $s_{16} = 2^{15} s_{15} + 2^{17} s_{13} + 2^{21} s_{10} + 2^{20} s_4 + (1 + 2^8) s_0 \bmod(2^{31} - 1)$
2. if $s_{16} = 0$ then set $s_{16} = 2^{31} - 1$
3. $(s_{16}, s_{15}, \dots, s_2, s_1) \leftarrow (s_{15}, s_{14}, \dots, s_1, s_0)$.

Bitreorganization()

1. $X_0 = s_{15H} \llcorner s_{14L}$
2. $X_1 = s_{11L} \llcorner s_{9H}$
3. $X_2 = s_{7L} \llcorner s_{5H}$
4. $X_3 = s_{2L} \llcorner s_{0H}$,

where s_{iH} is the high 16 bits of the cell s_i and s_{jL} is the low 16 bits of the cell s_j .

$F(X_0, X_1, X_2)$

1. $W = (X_0 \llcorner R_1) \llcorner R_2$ is the FSM output
2. $W_1 = R_1 \llcorner X_1$
3. $W_2 = R_2 \llcorner X_2$
4. $R_1 = S(L_1(W_{1L} \llcorner W_{2H}))$
5. $R_2 = S(L_2(W_{2L} \llcorner W_{1H}))$,

where $S = (S_0, S_1, S_0, S_1)$ is the 4 parallel S-boxes which are the same as those used in the previous ZUC-128 and L_1 and L_2 are the two MDS matrices used in the ZUC-128. The ZUC-256 stream cipher generates a 32-bit keystream word at each time instant.

KeystreamGeneration()

1. Bitreorganization()
2. $Z = F(X_0, X_1, X_2) \llcorner X_3$
3. LFSRWithworkMode().

ZUC-256 generates from 20000-bit up to 2^{32} -bit keystream for each frame; after that a key/IV re-synchronization is performed with the key/constants fixed and the IV changing into a new value.

The MAC generation algorithm of ZUC-256 is as follows. Let $M = (m_0, m_1, \dots, m_{l-1})$ be the l -bit length plaintext message and the size t of the tag is selectively to be of 32, 64 and 128 bits.

MAC_Generation(M)

1. Let ZUC-256 produce a keystream of $L = d \frac{l}{32} e + 2 \frac{t}{32}$ words. Denote the keystream bit string by $z_0, z_1, \dots, z_{32L-1}$, where z_0 is the most significant bit of the first output keystream word and z_{31} is the least significant bit of the first keystream word.

2. Initialize $Tag = (z_0, z_1, \dots, z_{t-1})$
3. for $i = 0$ to $l-1$ do
 - { let $W_i = (z_{t+i}, \dots, z_{i+2t-1})$
 - { if $m_i = 1$ then $Tag = Tag \oplus W_i$
4. $W_l = (z_{l+t}, \dots, z_{l+2t-1})$
5. $Tag = Tag \oplus W_l$
6. return Tag

For the different sizes of the MAC tag, to prevent the forgery attack, the constants are specified as follows.

1. for the tag size of 32 bits, the constants are

$$\begin{aligned}
 d_0 &= 1100100 \\
 d_1 &= 1000011 \\
 d_2 &= 1111010 \\
 d_3 &= 0101010 \\
 d_4 &= 0010001 \\
 d_5 &= 0000101 \\
 d_6 &= 1010001 \\
 d_7 &= 1000010 \\
 d_8 &= 0011010 \\
 d_9 &= 0110001 \\
 d_{10} &= 0011000 \\
 d_{11} &= 1100110 \\
 d_{12} &= 0010100 \\
 d_{13} &= 0101110 \\
 d_{14} &= 0000001 \\
 d_{15} &= 1011100.
 \end{aligned}$$

2. for the tag size of 64 bits, the constants are

$$\begin{aligned}
 d_0 &= 1100101 \\
 d_1 &= 1000011 \\
 d_2 &= 1111011 \\
 d_3 &= 0101010 \\
 d_4 &= 0010001
 \end{aligned}$$

$d_5 = 0000101$
 $d_6 = 1010001$
 $d_7 = 1000010$
 $d_8 = 0011010$
 $d_9 = 0110001$
 $d_{10} = 0011000$
 $d_{11} = 1100110$
 $d_{12} = 0010100$
 $d_{13} = 0101110$
 $d_{14} = 0000001$
 $d_{15} = 1011100.$

3. for the tag size of 128 bits, the constants are

$d_0 = 1100101$
 $d_1 = 1000011$
 $d_2 = 1111010$
 $d_3 = 0101010$
 $d_4 = 0010001$
 $d_5 = 0000101$
 $d_6 = 1010001$
 $d_7 = 1000010$
 $d_8 = 0011010$
 $d_9 = 0110001$
 $d_{10} = 0011000$
 $d_{11} = 1100110$
 $d_{12} = 0010100$
 $d_{13} = 0101110$
 $d_{14} = 0000001$
 $d_{15} = 1011100.$

The test vectors of the ZUC-256 stream cipher for the keystream generation phase are as follows.

1. let $K_i = 0x00$ for $0 \leq i < 31$ and $IV_i = 0x00$ for $0 \leq i < 15$, then the first 20 keystream words are
 - 0234e932, f0c22292, 38853662, aa624def, 7f99a4c7,
 - e47a0282, b2fde38d, f4cb89c5, 3c17ab18, 87ef5093,
 - 15c53d45, af1de542, 7d278dbb, 839af54e, e9375674,
 - 01d3207e, 7f1d6fb3, b5770472, c4f98e41, 637788d9

2. let $K_i = 0xff$ for $0 \leq i < 31$ and $IV_i = 0xff$ for $0 \leq i < 15$, then the first 20 keystream words are
- 3985e2af, 3533d429, 338580f0, e0d80ce9, 0649e5be,
 - 4961b8a2, d23a44d3, 9c18ce98, 75f7c424, 082ecf47,
 - e1d384b8, 91ace320, e46f0b16, cf903c77, f097f1a9,
 - 4bcb2079, fb5c6cc1, 6e9f3e05, 6eff3261, 89ea0373

The test vectors of the ZUC-256 stream cipher for the tag authentication phase are as follows.

1. let $K_i = 0x00$ for $0 \leq i < 31$ and $IV_i = 0x00$ for $0 \leq i < 15$, $M = 0x \underbrace{00, \{Z, 00\}}_{100}$ with the length $l = 400$ -bit, then the 32-bit tag, 64-bit tag and 128-bit tag are
 - The 32-bit tag is d51f12fc
 - The 64-bit tag is 3f4aaa58 99158f4a
 - The 128-bit tag is cf4bc324 7d0f6ae5 ce498d54 4556c247
2. let $K_i = 0x00$ for $0 \leq i < 31$ and $IV_i = 0x00$ for $0 \leq i < 15$, $M = 0x \underbrace{11, \{Z, 11\}}_{1000}$ with the length $l = 4000$ -bit, then the 32-bit tag, 64-bit tag and 128-bit tag are
 - The 32-bit tag is 55f6c1a1
 - The 64-bit tag is 972be021 f8152288
 - The 128-bit tag is f9d9a922 37cba79b 42394e2c 3df7a9e4
3. let $K_i = 0xff$ for $0 \leq i < 31$ and $IV_i = 0xff$ for $0 \leq i < 15$, $M = 0x \underbrace{00, \{Z, 00\}}_{100}$ with the length $l = 400$ -bit, then the 32-bit tag, 64-bit tag and 128-bit tag are
 - The 32-bit tag is 5aea7964
 - The 64-bit tag is 11720876 83515f4b
 - The 128-bit tag is 70469592 61c0dc2e e4f88400 5f1e4368
4. let $K_i = 0xff$ for $0 \leq i < 31$ and $IV_i = 0xff$ for $0 \leq i < 15$, $M = 0x \underbrace{11, \{Z, 11\}}_{1000}$ with the length $l = 4000$ -bit, then the 32-bit tag, 64-bit tag and 128-bit tag are
 - The 32-bit tag is 06637506
 - The 64-bit tag is 7a6cfe5c 74615bfe
 - The 128-bit tag is dd3a4017 357803a5 1c3fb9a5 7a96feda

The security claim of the ZUC-256 stream cipher with the new initialization scheme is the 256-bit security in the 5G application setting. For the forgery attacks on the authentication part, the security level is the same as the tag size and the IV is not allowed to be re-used. If the tag verification failed, no output should be generated.

3 The Analysis Related to the New Change

In this section, we will present the cryptanalysis of the new initialization scheme, other aspects of the security analysis that is not effected by the newly introduced change will remain the same as before, and will not cover here.

3.1 Differential Attacks

Chosen IV/Key attacks aim at the initialization stage of a stream cipher. For a good stream cipher, after the initialization, each bit of the IV/Key should contribute to each bit of the internal states, and any difference in the IV/Key will result in an almost-uniform and unpredictable difference in the internal states. In stream cipher domain, it is more frequent to change the IV than to change the key. And since the IV is known to the public, so the chosen-IV attack is more feasible. The main idea of chosen-IV attack is to choose some differences in some IV bits and study the propagation of the differences during the initialization of the cipher. To evaluate the diffusion of the input difference in IV effectively, we

Table 1. Least number of rounds that every bit is inserted into FSM

Location	Diffusion rounds
0	6 6 6 6 6 6 6 6 7 7 7 7 7 7 7 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6
1	7 7 7 7 7 7 7 7 8 8 8 8 8 8 8 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7
2	8 8 8 8 8 8 8 8 9 9 9 9 9 9 9 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
3	9 9 9 9 9 9 9 9 10 10 10 10 10 10 10 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9
4	7 7 7 7 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 7 7 7 7 7 7 7 7 7 7 7
5	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 7 7 7 7 8 8 8 8 8 8 8 8 8 8 8 8 8
6	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 8 8 8 8 9 9 9 9 9 9 9 9 9 9 9 9 9
7	3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
8	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
9	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3
10	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
11	3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
12	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
13	5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3
14	6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
15	6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5

make the following two assumptions:

1. If the input difference to the FSM is not zero, then the output difference of FSM is all 1. As L is an MDS matrix and S is non-linear permutation, the difference is diffused sufficiently and faster than the LFSR.
2. The modular addition operation is reduced to be the traditional xor. The diffusion of difference in modular addition is related to the values of states.

Meanwhile, the modular addition can be seen as the xor with carry. Thus, it is reasonable to follow this assumption to a certain extent.

In order to evaluate the property of initialization stage comprehensively, we give three kinds of analysis.

Firstly, we want to know the minimum number of iteration steps to guarantee that each bit of feedback is influenced by each bit in the initialization state. We divide the initialization state into $16 \times 31 = 496$ bits and test the least number of rounds that each bit is inserted into FSM. The obtained results are shown in Table 1, where 'Location' denotes the index i of s_i and the leftmost location is denoted by 15. Combining with the key/IV loading procedure, we can conclude that the difference of IV is inserted to FSM after at most four rounds and the memory cells are influenced after at most five rounds.

The conclusion mentioned above is tested under two assumptions and may be different to the real results. We randomly choose 2^{11} (K, IV) pairs to test the diffusion property in practice. In details, just exhaustively test all the possible differences for i -th ($0 \leq i \leq 15$) word of IV to get the maximum iteration steps for causing difference in memory cells R_1 and R_2 . The results of experiments are summarized as Table 2. We can see that the memory cells are influenced after

Table 2. Maximum steps to lead difference in R_1 and R_2

i	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
R_1	1	2	3	4	2	3	4	5	1	2	3	4	2	3	4	5
R_2	2	3	4	5	1	2	3	4	2	3	4	5	1	2	3	4

at most five rounds from Table 2 and the result matches the above conclusion from Table 1.

Secondly, the minimum number of iterations to guarantee that each bit of the register state is influenced by each bit of initialization state will be focused. In a word, if the input to FSM is different, then the state of the feedback word s_{15} will have some difference in the next round. The differential state will be shifted to the rightmost location in the next 15 rounds and all the states will be affected.

We have also made some experiments to evaluate this diffusion property in practice. For the injected difference position on each bit of IV, we have chosen 2^{22} (K, IV) pairs to get the least number of steps that all the register states are influenced. The experimental results show that each bit of register state is affected by each bit of IV after at most 19 rounds.

Thirdly, we will investigate the differential characteristic aspect of the initialization scheme when the injected difference positions covering all the possible key and IV loading positions.

We have searched the minimum number of active S-box of the initialization scheme under the simplification that the $2^{31} - 1$ addition operation of the LFSR

Table 3. The differences of the LFSR in each round of iteration

Index	K_2	K_{18}	K_{26}	K_{22}	K_{30}	Index	K_2	K_{18}	K_{26}	K_{22}	K_{30}
0	0x81	0x80	0x80	0x0c	0x00	22	0x88	0x80	0x80	0x44	0x48
1	0x02	0x00	0x00	0x10	0x10	23	0x30	0x30	0x30	0x01	0x83
2	0x01	0x00	0x00	0x08	0x08	24	0x11	0x10	0x10	0x08	0x89
3	0x04	0x00	0x00	0x20	0x20	25	0x06	0x00	0x00	0x30	0x30
4	0x42	0x40	0x40	0x12	0x14	26	0x07	0x00	0x00	0x38	0x38
5	0x08	0x00	0x00	0x40	0x40	27	0xc0	0xc0	0xc0	0x06	0x0c
6	0x21	0x20	0x20	0x09	0x0a	28	0x0b	0x00	0x00	0x58	0x58
7	0x41	0x40	0x40	0x0a	0x0c	29	0xa0	0xa0	0xa0	0x05	0x0a
8	0x83	0x80	0x80	0x1c	0x10	30	0x28	0x20	0x20	0x41	0x42
9	0x85	0x80	0x80	0x2c	0x20	31	0x0a	0x00	0x00	0x50	0x50
10	0x14	0x10	0x10	0x20	0xa1	32	0x82	0x80	0x80	0x14	0x18
11	0x09	0x00	0x00	0x48	0x48	33	0x24	0x20	0x20	0x21	0x22
12	0x10	0x10	0x10	0x00	0x81	34	0x0d	0x00	0x00	0x68	0x68
13	0x20	0x20	0x20	0x01	0x02	35	0x84	0x80	0x80	0x24	0x28
14	0x18	0x10	0x10	0x40	0xc1	36	0x48	0x40	0x40	0x42	0x44
15	0x89	0x80	0x80	0x4c	0x40	37	0x0c	0x00	0x00	0x60	0x60
16	0x03	0x00	0x00	0x18	0x18	38	0x12	0x10	0x10	0x10	

0x10

Table 4 gives the difference propagation of the 16 cells of the LFSR after i rounds of iteration ($i = 1, 2, \dots, 27$) in a step-by-step manner. It is easy to see that the memory cells R_1 and R_2 have no difference even after 11 rounds, thus the differences $C-H$ are generated only from the $2^{31} - 1$ addition operation. We expect that the state cells s_{15} and s_{14} will have good differential randomness after 48 rounds. Hence, we believe that, after 49 rounds of iteration, the difference in the first 32-bit keystream word will be fairly random and unpredictable. Note that the above analysis will naturally be converted into a related key attack scenario, which is difficult, in stream cipher domain, to detect the related key pairs given only the corresponding keystream segments with the randomly generated IVs.

From the above analysis, we could conclude that the new initialization scheme of ZUC-256 could provide the 256-bit security in 5G application settings with a large expected security margin.

4 Conclusions

In this paper, we have presented the details of a new initialization scheme with 48 rounds for the ZUC-256 stream cipher that works with the 128-bit initialization vector. Any cryptanalysis of the new initialization scheme is welcome.

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